## Cambridge International Examinations

Cambridge International General Certificate of Secondary Education

## CANDIDATE NAME



CENTRE NUMBER


CANDIDATE NUMBER

Candidates answer on the Question Paper.
Additional Materials: Electronic calculator

## READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.
Write in dark blue or black pen.
You may use an HB pencil for any diagrams or graphs.
Do not use staples, paper clips, glue or correction fluid.
DO NOT WRITE IN ANY BARCODES.
Answer all the questions.
Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.
The use of an electronic calculator is expected, where appropriate.
You are reminded of the need for clear presentation in your answers.
At the end of the examination, fasten all your work securely together.
The number of marks is given in brackets [ ] at the end of each question or part question.
The total number of marks for this paper is 80 .

## Mathematical Formulae

## 1. ALGEBRA

## Quadratic Equation

For the equation $a x^{2}+b x+c=0$,

$$
x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a} .
$$

Binomial Theorem

$$
(a+b)^{n}=a^{n}+\binom{n}{1} a^{n-1} b+\binom{n}{2} a^{n-2} b^{2}+\ldots+\binom{n}{r} a^{n-r} b^{r}+\ldots+b^{n},
$$

where $n$ is a positive integer and $\binom{n}{r}=\frac{n!}{(n-r)!r!}$.

## 2. TRIGONOMETRY

Identities

$$
\begin{gathered}
\sin ^{2} A+\cos ^{2} A=1 \\
\sec ^{2} A=1+\tan ^{2} A \\
\operatorname{cosec}^{2} A=1+\cot ^{2} A
\end{gathered}
$$

Formulae for $\triangle A B C$

$$
\begin{gathered}
\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C} \\
a^{2}=b^{2}+c^{2}-2 b c \cos A \\
\Delta=\frac{1}{2} b c \sin A
\end{gathered}
$$

1 (a) On the axes below, sketch the graph of $y=3 \cos 2 x-1$, for $0^{\circ} \leqslant x^{\circ} \leqslant 360^{\circ}$.

(b) Given that $y=4 \sin 6 x$, write down
(i) the amplitude of $y$,
(ii) the period of $y$.

$$
\begin{aligned}
& \mathrm{p}(x)=2 x^{3}+5 x^{2}+4 x+a \\
& \mathrm{q}(x)=4 x^{2}+3 a x+b
\end{aligned}
$$

Given that $\mathrm{p}(x)$ has a remainder of 2 when divided by $2 x+1$ and that $\mathrm{q}(x)$ is divisible by $x+2$,
(i) find the value of each of the constants $a$ and $b$.

Given that $\mathrm{r}(x)=\mathrm{p}(x)-\mathrm{q}(x)$ and using your values of $a$ and $b$,
(ii) find the exact remainder when $\mathrm{r}(x)$ is divided by $3 x-2$.

3 The coefficient of $x^{2}$ in the expansion of $(2-x)(3+k x)^{6}$ is equal to 972 . Find the possible values of the constant $k$.

4 (i) Write $x^{2}-9 x+8$ in the form $(x-p)^{2}-q$, where $p$ and $q$ are constants.
(ii) Hence write down the coordinates of the minimum point on the curve $y=x^{2}-9 x+8$.
(iii) On the axes below, sketch the graph of $y=\left|x^{2}-9 x+8\right|$, showing the coordinates of the points where the curve meets the coordinate axes.

(iv) Write down the value of $k$ for which $\left|x^{2}-9 x+8\right|=k$ has exactly 3 solutions.


The diagram shows a circle with centre $O$ and radius $r \mathrm{~cm}$. The minor arc $A B$ is such that angle $A O B$ is $\theta$ radians. The area of the minor sector $A O B$ is $48 \mathrm{~cm}^{2}$.
(i) Show that $\theta=\frac{96}{r^{2}}$.
(ii) Given that the minor arc $A B$ has length 12 cm , find the value of $r$ and of $\theta$.
(iii) Using your values of $r$ and $\theta$, find the area of the shaded region.

6 A curve has equation $y=\frac{\ln \left(2 x^{2}+3\right)}{5 x+2}$.
(i) Show that $\frac{\mathrm{d} y}{\mathrm{~d} x}=-\frac{5}{4} \ln 3$ when $x=0$.
(ii) Hence find the equation of the tangent to the curve at the point where $x=0$.

7 (a) Express $2+3 \lg x-\lg y$ as a single logarithm to base 10 .
(b) (i) Solve $6 x+7-\frac{3}{x}=0$.
(ii) Hence, given that $6 \log _{a} 3+7-3 \log _{3} a=0$, find the possible values of $a$.
$8 \quad$ (i) Find $\frac{\mathrm{d}}{\mathrm{d} x}\left(5 x^{2}+4\right)^{\frac{3}{2}}$.
(ii) Hence find $\int x\left(5 x^{2}+4\right)^{\frac{1}{2}} \mathrm{~d} x$.

Given that $\int_{0}^{a} x\left(5 x^{2}+4\right)^{\frac{1}{2}} \mathrm{~d} x=\frac{19}{15}$,
(iii) find the value of the positive constant $a$.
$9 \quad$ Variables $s$ and $t$ are such that $s=4 t+3 \mathrm{e}^{-t}$.
(i) Find the value of $s$ when $t=0$.
(ii) Find the exact value of $t$ when $\frac{\mathrm{d} s}{\mathrm{~d} t}=2$.
(iii) Find the approximate increase in $s$ when $t$ increases from $\ln 5$ to $\ln 5+h$, where $h$ is small.

10 Particle $A$ is at the point with position vector $\binom{2}{-5}$ at time $t=0$ and moves with a speed of $10 \mathrm{~ms}^{-1}$ in the same direction as $\binom{3}{4}$.
(i) Given that $A$ is at the point with position vector $\binom{38}{a}$ when $t=6 \mathrm{~s}$, find the value of the constant $a$. [3]

Particle $B$ is at the point with position vector $\binom{16}{37}$ at time $t=0$ and moves with velocity $\binom{4}{2} \mathrm{~ms}^{-1}$.
(ii) Write down, in terms of $t$, the position vector of $B$ at time $t \mathrm{~s}$.
(iii) Verify that particles $A$ and $B$ collide.
(iv) Write down the position vector of the point of collision.

11 (a) $\mathrm{f}(x)=3-\cos 2 x$ for $0 \leqslant x \leqslant \frac{\pi}{2}$.
(i) Write down the range of f .
(ii) Find the exact value of $\mathrm{f}^{-1}(2.5)$.
(b) $\mathrm{g}(x)=3-x^{2} \quad$ for $x \in \mathbb{R}$.

Find the exact solutions of $\mathrm{g}^{2}(x)=-6$.

## BLANK PAGE

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (UCLES) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

To avoid the issue of disclosure of answer-related information to candidates, all copyright acknowledgements are reproduced online in the Cambridge International Examinations Copyright Acknowledgements Booklet. This is produced for each series of examinations and is freely available to download at www.cie.org.uk after the live examination series.

Cambridge International Examinations is part of the Cambridge Assessment Group. Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.

